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## OPTICAL PROPERTIES AND QUANTUM CONFINEMENT EFFECTS IN THE POROUS Si

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Определены спектры комплексов оптических функций матрицы пористого кремния r-Si для трех групп образцов с пористостью P=19, 31, 41, 50 и 60% (p<sup>+</sup>-тип), 57, 66 и 77% (p-тип) (A), 31 и 57 % (p<sup>+</sup>-тип), 54 и 64% (p-тип) (B) в области 1.5–5 эВ, 70 и 67% (C) в области 0–20 эВ, а также двух вариантов теоретических спектров нанокластеров nSi в области 1–10 эВ. Расчеты выполнены на основе известных экспериментальных спектров R и  $\epsilon_2$  с помощью модели Бруггемана, а также теоретических  $\epsilon_2$ . Спектры  $\epsilon_2$  разложены на элементарные компоненты. Определены энергии и вероятности переходов компонент. Установлены большие различия между спектрами объемного и матрицы пористого кремния, обусловленные квантовыми размерными эффектами.

The experimental  $\epsilon_2(E)$  spectra in the range 1 to 5 eV are known for 8 (the parameter P=19, 31, 41, 50 and 60%, p<sup>+</sup>-type; 57, 66 and 77%, p-type samples) [1] and 4 other samples (P=31 and 57 % for p<sup>+</sup>-type, 54 and 64% for p-type) [2] and also R(E) in the range 1 to 20 eV (P=70%, p-type) [3,4], but only two theoretical  $\epsilon_2$  spectra for the nanoclusters n-Si in the range 1 to 10 eV [5,6]. Using their results we calculated the spectra of the 7 variants of the other optical functions for PSi and r-Si and 2 variants of the theoretical spectra of the nanoclusters. The special computer programs are obtained using Bruggeman model for the PSi and integral Kramers-Kronig interrelations. Further, the  $\epsilon_2$  spectra were decomposed into the elemental components with the energy and oscillators strength using the method of unified Argand diagram [7].

For the first we discuss the results for the range 0 to 20 eV. The reflectivity  $R_{ef}(E)$  spectrum of the porous Si (PS) was measured in the range 2 to 20 eV on the samples with porous parameter  $P_0 \approx 0.70$  [3]. It was proved very weak ( $R < 0.15$ ) and smaller than for the volume Si (c-Si) 6 and 4.6 times in the 1–2 and 3–4 eV (Fig.1a,a'). The R(E) curve has the doublet band in the region 2.5 to 5 eV with the highly overlapped maxima at ~3.7 and 4.3 eV and the very wide and weak band at ~10.4 eV.

We calculate the full complex of the PS fundamental optical functions using the method of [7]. Only effective  $R_{ef}$  and  $\epsilon_{2ef}$  spectra are on the Fig.1 for shortness. The calculated values of effective optical functions are very small (Fig.1b').

The full complex of fundamental functions for the residue Si (r-Si) was calculated using the obtained

effective  $\epsilon_{2ef}$  and  $\epsilon_{1ef}$  PS spectra on the basis of the Bruggeman model (Fig.1.a,b;  $P = P_0(1 - P_0)^{-1} = 2.33$ ,  $P_0 = 0.70$ ). The error of  $P_0$  is usual to 0.01–0.03. Therefore the calculation were carried out also for the P=2.0.

The calculated  $\epsilon_2$  and  $\epsilon_1$  r-Si spectra content one very wide band with the maxima at ~3.7 eV ( $\epsilon_2$ ) and one peak at ~3.5 eV and minimum at ~4.25 eV ( $\epsilon_1$ ) in the energy range 2.5 to 6 eV.

The reflectivity curve of r-Si have the doublet from the maximum at ~4.55 eV and weak peak at ~3.8 eV in the energy range 1–5 eV. It decreased in the higher energy to the minimum at ~7.7 eV and consists of very wide band with the two maxima at ~10.4 and ~13.4 eV. The transition from P=2.33 to P=2 is diminished the reflectivity in the full energy region 0 to 20 eV.

The theoretical  $\epsilon_2$  spectra are known for the clusters of 83 [5] and 60 atoms [6] (Fig.1b). We calculate the spectra of other optical functions using the results of [5,6] (Fig.1a,b). The most intensive longwavelength theoretical  $\epsilon_2$  band of Si<sub>83</sub> cluster is correlated very well in the energy range 3 to 5 eV with the our data for the r-Si  $\epsilon_2$ .

It is very significant to establish the value of the difference between r-Si and c-Si optical spectra in the wide energy range. The longwavelength c-Si very intensive reflectivity is beginning from the two maxima at ~3.4 and ~4.5 eV but their analogs of r-Si are displaced in the higher energy range on the ~0.4 and ~0.05 eV. The c-Si R(E) have very intensive and wide band in the range 5 to 8 eV instead of r-Si wide and deep minimum and very strong monotonic decreasing in the range 10 to 20 eV instead of the intensive very wide doublet r-Si band. The

analogous peculiarities are observed in the other c-Si and r-Si spectra. The curves of  $R$ ,  $\epsilon_1$ ,  $\epsilon_2$  for r-Si are displaced in the higher energy range from the data of c-Si. Therefore this phenomena is theoretically caused by the quantum confinement effects of PS.

Further we discuss the results for the range 1 to 5 eV. The experimental  $\epsilon_2$  spectrum of unetched silicon (c-Si) shows two prominent maxima at about 3.44 and 4.25 eV. In going from c-Si to PS,  $\epsilon_{2ef}$  decreases by tens of times, the longer wavelength maximum (3.44 eV) disappears, and the shorter wavelength maximum becomes much broader. The calculated  $\epsilon_2$  spectra of r-Si also contain no maximum around 3.44 eV. At  $P=0.57$ , the  $\epsilon_1$  spectrum of r-Si shows a maximum centered around 4.2 eV and a

broad shoulder at about 3.8 eV. With increasing porosity, the relative intensity of the shoulder increases. The  $k$  and  $n$  spectra show similar features.

The table lists the parameters obtained by decomposing the permittivity spectra of c-Si ( $P=0$ ) and r-Si ( $P=0.57, 0.66, 0.77$ ). The strongest maxima (5 and 1) in the decomposed  $\epsilon_2$  spectrum of c-Si are also present in the integral curve. In addition, the spectrum contains one rather strong band (3) and four weak features (2, 4, 6, 7). The decomposed  $\epsilon_2$  spectrum of r-Si with  $P=0.57$  shows the same seven components as are present in the spectrum of c-Si. Components 3–6 are shifted to higher energies by 0.10–0.16 eV, component 1 is shifted to lower energies by  $\sim 0.2$  eV, and components 2 and 7 undergo shift.

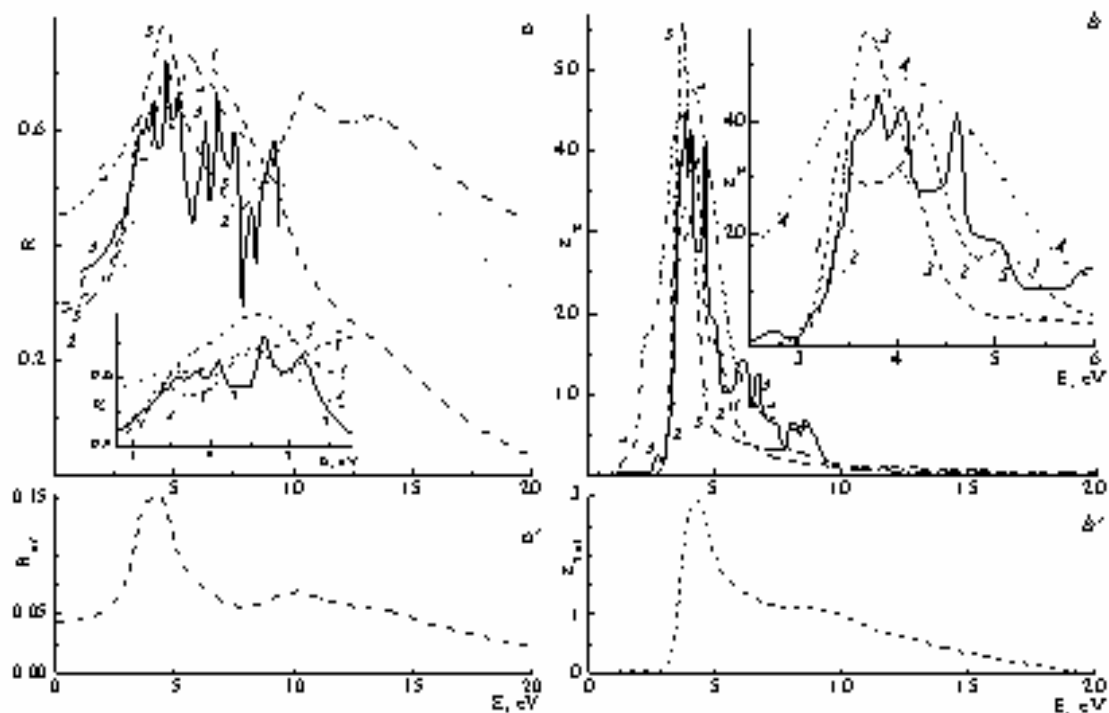


Fig. 1.  $R(a)$ ,  $R_{ef}(a')$ ,  $\epsilon_2(b)$ ,  $\epsilon_{2ef}(b')$  spectra in the energy range 0–20 eV for the c-Si [7] (1), r-Si of the PS samples for the  $P=2.0$  (2) and 2.33 (3), and for clusters  $Si_{60}$  (4) and  $Si_{83}$  (5), calculated using the theoretical  $\epsilon_2$  spectra [5,6]; on the inserts are spectra in the range 2 to 6 eV

The band area  $S_i$  is proportional to the transition strength. In going from c-Si to r-Si with  $P=0.57$ , the areas of the strongest bands (5 and 1) decrease by about a factor of 2, while the intensity of band 3 increases by about 20% (for these bands, the accuracy in  $S_i$  is about  $\pm 10\%$ ). Increasing the porosity to 0.66 reduces the intensity of components 5–7 to zero but has little or no effect on the intensity of components 1, 3, 4. At  $P=0.77$ , component 3 is almost indiscernible, while components 1 and 2 persist. The values of  $H_i$  for components 1 and 2 in the spectrum of r-Si are 2.5 times higher than those for c-Si. It is probably for this reason that component 2 was difficult to detect at  $P=0.66$ . The very low intensity of some components at  $P=0.66$  and 0.77 made difficult to detect them, and the effect of porosity on their energy position could not be analyzed. The total area of all the components is 56.1 at  $P=0$ , 47.3 at  $P=0.57$ , 22.8 at  $P=0.66$ , and 9.7 at  $P=0.77$ .

Thus, relatively low porosity ( $P=0.57$ ) drastically reduces the intensity of components 5, 1, and 7 and increases that component 2. Increasing the porosity to 0.66 has little effect on components 1–4 but leads to the disappearance of the other components (5–7). At a still higher porosity ( $P=0.77$ ), components 4 and 3 are missing, while the longest wavelength components 1 and 2 persist. In going from c-Si to r-Si, the total strength of the transitions in the range 3–5 eV decreases: by  $\sim 20\%$  at  $P=0.57$ , by about a factor of 2.5 at  $P=0.66$ , and by a factor of 5.8 at  $P=0.77$ .

The above spectra of r-Si were calculated for PS samples consisting of only two media: pores and r-Si. However, the PS surface may be coated with amorphous Si (a-Si),  $SiO_x$ , or  $SiH_x$ . the thickness of such films depends on the conductivity of the parent c-Si, PS preparation procedure, and storage conditions, and their effect on the experimental spectra of PS and calculated

spectra of r-Si depends on their optical properties [8–10]. SiO<sub>2</sub> and SiO<sub>1.5</sub> have high transmittances for E<10 eV. The reflectivity spectrum of a-SiO shows a very broad (2–8 eV), weak band centered around 4 eV (R=0.15). The spectra of a-Si and a-Si:H contain a very broad band between 2 and 12 eV, centered around 6 eV. Analysis of these features (energy position, halfwidth, and Rmax) for

the films in question on the PS surface indicates that such films have a weak effect on the experimental  $\epsilon_{2ef}$  spectra of PS [1] and calculated spectra r-Si. Note that Ferrieu et al. [1] also pointed out that thin (<1 nm) oxide films had no effect on  $\epsilon_{2ef}$ .

Table. Parameters E<sub>i</sub> (eV), H<sub>i</sub>, I<sub>i</sub>, and S<sub>i</sub> (eV) obtained by decomposing the  $\epsilon_2$  spectra of c-Si (P = 0) and r-Si (P = 0.57, 0.66, 0.77)

N	E <sub>i</sub>				H <sub>i</sub>				I <sub>i</sub>				S <sub>i</sub>			
	0.00	0.57	0.66	0.77	0.00	0.57	0.66	0.77	0.00	0.57	0.66	0.77	0.00	0.57	0.66	0.77
1	3.44	3.24	3.34	3.21	0.20	0.53	0.40	0.53	22.90	4.60	6.30	3.90	7.06	3.70	3.80	3.10
2	3.60	3.60	–	3.63	0.20	0.49	–	0.48	7.50	8.40	–	7.80	2.30	6.20	–	5.60
3	3.78	3.90	3.80	3.91	0.47	0.58	0.50	0.33	18.50	18.60	18.00	2.00	13.14	16.20	13.6	1.00
4	4.04	4.18	4.15	–	0.41	0.27	0.35	–	6.15	11.50	10.10	–	3.86	4.80	5.40	–
5	4.25	4.41	–	–	0.44	0.60	–	–	35.90	14.60	–	–	24.03	13.20	–	–
6	4.50	4.60	–	–	0.24	0.27	–	–	4.00	5.30	–	–	1.47	2.20	–	–
7	4.85	4.80	–	–	0.60	0.20	–	–	4.70	3.20	–	–	4.26	1.00	–	–

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